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The point values for each question is given within []. The total number of points for this assignment is 25 .

1. Consider graph $G$ :

(a) Provide an adjacency matrix for the graph.
(b) Compute the number of paths of length 3 between vertex 3 and vertex 4, and then list each path.
(c) Does $G$ contain an Euler path? Why or why not?
(d) Is $G$ Hamiltonian? Why or why not?
(e) We can use Dijkstra's Algorithm to compute the shortest path from vertex 0 to all the other vertices in graph $G$. Complete each of the tables below that represent the state of the data structures used by Dijkstra's algorithm each time a vertex's shortest distance from vertex 0 becomes known.

| Step 1 | Vertex | Known | Distance | Previous |
| :---: | :---: | :---: | :---: | :---: |
|  | 0 | True | 0 | -1 |
|  | 1 | False | 3 | 0 |
|  | 2 | False | 4 | 0 |
|  | 3 | False | $\infty$ | -1 |
|  | 4 | False | $\infty$ | -1 |
|  | 5 | False | $\infty$ | -1 |
| Step 2 | Vertex | Known | Distance | Previous |
|  | 0 | True | 0 | -1 |
|  | 1 |  |  |  |
|  | 2 |  |  |  |
|  | 3 |  |  |  |
|  | 4 |  |  |  |
|  | 5 |  |  |  |
| Step 3 | Vertex | Known | Distance | Previous |
|  | 0 | True | 0 | -1 |
|  | 1 |  |  |  |
|  | 2 |  |  |  |
|  | 3 |  |  |  |
|  | 4 |  |  |  |
|  | 5 |  |  |  |


| Step 4 | Vertex | Known | Distance | Previous |
| :---: | :---: | :---: | :---: | :---: |
|  | 0 | True | 0 | -1 |
|  | 1 |  |  |  |
|  | 2 |  |  |  |
|  | 3 |  |  |  |
|  | 4 |  |  |  |
|  | 5 |  |  |  |
| Step 5 | Vertex | Known | Distance | Previous |
|  | 0 | True | 0 | -1 |
|  | 1 |  |  |  |
|  | 2 |  |  |  |
|  | 3 |  |  |  |
|  | 4 |  |  |  |
|  | 5 |  |  |  |
| Step 6 | Vertex | Known | Distance | Previous |
|  | 0 | True | 0 | -1 |
|  | 1 |  |  |  |
|  | 2 |  |  |  |
|  | 3 |  |  |  |
|  | 4 |  |  |  |
|  | 5 |  |  |  |

2. What is the maximum number of edges in a simple undirected graph with eight vertices? Justify your answer.
3. Which of the graphs in Figure 9.2.11 of your textbook are isomorphic? Produce the bijection for one pair of isomorphic graphs.
4. How many edges does $K_{10}$ have? Justify your answer.
