$\qquad$
The point values for each question appear within []. The total number of points for this assignment is 5 .
[5] 1. Let $A, B$, and $C$ all be subsets of universal set $U$. Use basic definitions to prove

$$
(A \cup B) \times C \subseteq(A \times C) \cup(B \times C)
$$

Hint: Your proof necessarily will involve statements such as

$$
A \cup B=\{x \mid x \in A \vee x \in B\} \quad \text { (Definition of union) }
$$

and

$$
A \times C=\{(x, y) \mid x \in A \wedge y \in C\} \quad \text { (Definition of Cartesian product) }
$$

and in your proof you will invoke the distributive law from the basic logic laws in Chapter 3.

|  | Statement | Reason |
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